Physical Design Automation for High-Density 3D Power Module Layout Synthesis and Optimization

Imam Al Razi\(^a\), Quang Le\(^b\), H. Alan Mantooth\(^b\), Yaruí Peng\(^a\)

\(^a\) Computer Science and Computer Engineering Department, \(^b\) Electrical Engineering Department
University of Arkansas, Fayetteville, AR, US
ialrazi@uark.edu, yrpeng@uark.edu

Abstract—With the on-going trend of electrification of transport, ultra-high-density power electronics with advanced 2.5D and 3D packaging are drawing attention. At present, the power module design is still a manual and time-consuming procedure. Floorplanning, placement, routing, and parasitic extraction need to be performed carefully to enhance performance without sacrificing reliability. Inspired by design automation tools for VLSI circuits, design automation tools for power electronics can dramatically reduce the engineering time and costs. As 3D power module fabrication is on the horizon to further improve power density, in this work, we present physical design algorithms to automate the 3D power module layout synthesis and optimization. Hierarchical corner stitch and constraint graphs are used to guarantee manufacturable layouts. Our algorithms are generic and scalable to integrate heterogeneous components with multiple devices and routing layers into a single power module. We demonstrate the improvement in the electro-thermal performance of a half-bridge 3D power module over a 2D counterpart. Also, the effectiveness and efficiency of our algorithms are demonstrated using real-world 3D power module designs.

Keywords—PowerSynth, corner stitch, constraint graph, 3D Multi-Chip Power Module, layout optimization

I. INTRODUCTION

To satisfy the increasing demands from automobiles, telecommunications, aerospace, and consumer electronics industries, next-generation power conversion systems, i.e., inverters and converters, need to be designed with high power density [1,2]. As power modules are key components of all the power converter systems, high-density power module design methodology is a critical research problem in the power electronics society. Significant improvement of power module efficiency has been achieved with the wide bandgap (WBG) power semiconductor devices. Therefore, power module physical design is getting increasingly more complex. Multi-chip power module (MCPM) designers are switching their focus from conventional 2D (single device and routing layer) package to 2.5D (single device layer with multiple routing layers on a planar substrate) and 3D (multiple devices and routing layers stacked on the same substrate) packaging [3–7]. The advanced packaging techniques enable heterogeneous component integration, reduce parasitics, shrink current loops, and improve efficiency with reduced volume and weight.

A circuit schematic of a simple half-bridge power module with a single MOSFET per switching position is shown in Fig. 1(b). Corresponding 2D and 3D layout structures are shown in Fig. 1(c). In traditional 2D MCPM designs, devices are wire-bonded with the traces to complete the electrical connection. Since the bonding wires contribute a good amount of parasitic inductance, at higher switching frequencies, these parasitic inductance give rise to undesirable voltage overshoots and ringing that leads to the generation of electromagnetic interference (EMI), which can cause device failures [8]. Besides, the aluminum bonding wires conducting high current are reliability weak points of the MCPMs [9]. To eliminate the reliability concerns about wire bonding technology and have a lower parasitic inductance, designers have come up with several packaging technologies like flip-chip wire-bondless modules [8], press-pack packaging [10], wafer-level chip-scale packaging [7]. In some of these designs, copper pin, metal post, shim material are used to connect the source terminal instead of bonding wires, which can eliminate the high drain-source voltage overshoot issue [9, 11]. In such designs, the gate and kelvin source are connected by bonding wires as they carry a smaller current compared to the power source connections. These types of packaging can be referred to as hybrid 3D packaging. All these 3D packaging concepts not
only reduce the electrical parasitics by minimizing the loop area but also improve thermal performance. This is because the double-sided cooling, as well as higher heat dissipation, is possible with the 3D technology. With these benefits, the 3D power module packaging technique becomes more attractive in the power electronics society.

In the power module manufacturing industry, to accelerate the current MCPM physical design flow and avoid the manual and iterative process, physical design automation has been initiated by many researchers. Several studies leveraging VLSI placement-and-routing (P&R) concepts are successfully applied to power module layout synthesis while considering the fundamental differences between VLSI and power electronics design [12–14]. Though progress is made on 2D power module design automation, a generalized 3D MCPM constraint-aware layout optimization methodology does not exist so far. In [13], a 2D power module layout is represented using the sequence-pair method, and a 1D binary string is used to randomize routing paths within the plane. Simplification is performed to reduce the problem size, which leads to inefficiency in handling complex geometry. A genetic algorithm (GA) based layout optimization method for the motor controller system is presented in [6]. Here, the 3D layout components are simplified as cubes and represented as a sequence group (an extension of sequence pair). GA operators are applied to the group to generate multiple solutions aiming at volume and connection length reduction. This method can explore very few solutions and does not guarantee the alignment of the layers. Also, the electro-thermal reliability of the solutions is not considered at all, which makes the approach inappropriate for 3D MCPM layout optimization.

In [12], a software tool called PowerSynth (GUI shown in Fig. 1(a)) is introduced that can help engineers to generate power module layouts from a draft design. It does not even require expertise in every aspect of the design flow. Further, with its built-in models for electrical and thermal evaluation, this tool can quickly analyze the electro-thermal performance of the layout without the need to run the finite element method (FEM) tools. A matrix-based methodology is used in this version to generate layout solutions during optimization. This methodology has been proven to be inefficient in layout generation due to iterative DRC-checking, and limited solution space. Several efforts are performed to overcome the limitations with the baseline tool and make the tool more generic, scalable, and efficient. As a part of these continuous research and development efforts, a new layout engine based on the corner stitching data structure with constraint graphs has been proposed in [14]. This new layout engine generates DRC-clean solutions with heterogeneous components and higher complexity. Since this is a planar version that can handle only 2D layouts and results in higher coordinate correlation, in [15], a hierarchical corner stitch data structure with hierarchical constraint propagation methodology is proposed to demonstrate the benefits of the hierarchical approach. The methodology randomizes constraint graph edge weights for generating solutions without considering connectivity or alignment, which causes loop inductance overestimation due to the increased length of the bonding wires. With this algorithm, both 2D and 2.5D power modules can be optimized in which a single device layer is allowed.

To reduce the complexity of 3D power module layout synthesis and optimization, data structure and algorithms have been updated in this work. The 2D-2.5D layout optimization approach has been extended to analyze and optimize the heterogeneous design with a multi-layered 3D structure. In this paper, we propose generic algorithms for 3D power module physical design automation that ensure the alignment among multiple-layers connected with vias. A case study has been demonstrated to highlight the improvements in the case of the 3D MCPM layout over the 2D. Also, electro-thermal optimization is performed on a hybrid 3D power module case to demonstrate the capability of high-density power module layout optimization.

II. PHYSICAL DESIGN AUTOMATION METHODOLOGY

A 3D power module is treated as a combination of multiple 2D layers connected with vias. An initial layout geometry with hierarchical placement and via connectivity information is taken as an input script, where each component is represented as a rectangle. The corner stitch data structure is used to create constraint graphs for each hierarchical level of each layer in the structure. Design constraints like minimum width, length, extension, enclosure, and spacing are considered in constraint graphs as edges. For generating layout solutions, constraint graph edge weights are manipulated by applying layout synthesis algorithms. The data structure and algorithms are described in this section.

A. Layout Representation

1) Corner Stitch: The basic corner stitch data structure [16] can represent a planar layout with non-overlapping tiles of two types: empty and solid. Each tile has four pointers to traverse neighbor tiles. A corner-stitched plane may have two variants: horizontal corner stitch (HCS), and vertical corner stitch (VCS). In the horizontal (vertical) corner stitch, each tile is horizontally (vertically) maximized. This rule has been proven to be very effective in finding design constraints for the layout. Since the algorithms associated with creating corner stitched planes are very efficient and finding design constraints for power module layout is a straight-forward task, this data structure is customized for power module layout representation.
2) Constraint Graph: A constraint graph is a technique to represent an inequality relationship between two vertices, where the edge weight is a minimum constraint value. Each corner-stitched tile can be mapped into two vertices in the graph connected with an edge weighting minimum constraint value associated with that tile. Two constraint graphs are generated: a horizontal constraint graph (HCG), and a vertical constraint graph (VCG). The HCG ensures horizontal minimum relative location among components, and the VCG maintains the vertical minimum relative location.

B. Layout Hierarchy

To represent the geometry and hierarchy of the 3D structure, a hierarchical tree structure is used. The root is considered as a reference node for the whole structure. Each group of connected layers in the 3D module is represented as a child of the root. For the example design with four layers bottom-to-top shown in Fig. 2(a), there are two groups of layers connected by vias: the first and the third as well as the second and the fourth layers. Therefore, there are two child nodes at the second level of the tree, where each child node has an outline of the connected layers and via locations. The tree is illustrated in Fig. 2(b) and the planar view of each node on the left subtree is shown in Fig. 3. Each layer node has a subtree consisting of components like trace, devices, leads, etc. In this example, each of the children of the root node has an outline of two connected layers and a via (Node A). Then layers with two traces (T1 and T2) and a via (V) are in Node 1 and Node 3. Since T1 has a device D, a child node (Node 2) is created from Node 1. Thus the whole structure can be represented hierarchically with a single tree.

Algorithm 1: Layout Generation Workflow

1. Read input script
2. Create a root node of the structure
3. Create group of connected layers sharing same vias
4. for each connected group do
   5. Create a sub-root (child of the root) with via locations
   6. for each layer in the sub-root do
      7. Create HCS and VCS
      8. Evaluate HCG and VCG
      9. Perform bottom-up constraint propagation
     10. Create HCG and VCG for sub-root node
   11. Evaluate root node
   12. Propagate evaluated locations to sub-roots
5. for each sub-root node do
   6. for each layer in the group do
      7. Perform top-down location propagation

C. Physical Design Methodology

An overview of the steps associated with the layout generation flow is presented in Algorithm 1.

Algorithm 2: Sub-root Node Creation

1. List1=list of all layers in the structure
2. List2=list of all vias in the structure
3. Via_connected_groups=map of connected layers and vias from List1 and List2
4. for each key, connected_layers_list in Via_connected_groups do
   5. Create a sub-root node
   6. Add information of all vias in the group
   7. Set as child of the root node
   8. Assign the root node as parent node
   9. for each layer in connected_layers_list do
      10. Set as child of the sub-root node
      11. Assign the sub-root node as parent node

1) Hierarchical Corner Stitch Creation: Each layer of the 3D structure has been treated as a 2D corner-stitched plane. Therefore, each child node of the sub-root nodes in the tree
has two corner stitch orientations. While creating hierarchical corner stitch planes (i.e., HCS, and VCS), two assumptions are considered:

1) Tile insertion is performed hierarchically. Before inserting a child component, the parent node components need to be inserted.

2) All tiles in any rectilinear polygon should be of the same type and need to be inserted sequentially.

In a hierarchical corner stitch data structure, each node has both foreground and background tiles. The background tiles are usually the copies from the parent node in the tree, and the foreground tiles are the newly inserted tiles and appended in the child node of the tree. These two varieties of tiles are required to find appropriate constraints among the components. Since this step is similar to in 2D layout handling, more details can be found in [15].

2) Constraint Graph Creation and Evaluation: Constraint graph creation starts from the leaf node of the tree structure. Since the parent node needs to have sufficient room for the child node, the child node constraint graphs are created, evaluated, and necessary constraint values are propagated to the parent node. From both corner stitched trees (i.e., HCS, VCS), the horizontal and vertical constraint graphs are created for each node in the tree (except the root and sub-root nodes) by mapping design constraints. The root and sub-root nodes are different from all other nodes in the tree as these nodes do not have corresponding corner-stitched planes while the others have. Therefore, for these nodes, the HCG and VCG are created using the propagated constraints from each sub-tree of the corresponding sub-root. A via propagation dictionary (a data structure to map key and value pair) is maintained for this purpose. Since via is declared as a component in one of the hierarchical levels of the tree, the coordinates associated with vias need to be propagated from that level to the sub-root node. The pseudocode associated with maintaining the via propagation dictionary is shown in Algorithm 3.

3) Bottom-up Constraint Propagation: The constraint graphs are evaluated by the longest path algorithm, and a bottom-up constraint propagation (algorithm shown in [15]) has been performed to respect the necessary design constraints from a child to the corresponding parent. An illustration of bottom-up constraint propagation is shown in Fig. 4. Here, HCG of each node is shown with some basic terminologies associated with the graph data structure. Each vertex refers to an x coordinate of the plane (shown in Fig. 3). The red edges are propagated edges, and corresponding weights are shown as a map of source node id and propagated value. For each node, the leftmost vertex is the source, and the rightmost vertex is the sink vertex. To preserve a fixed size for components, all dependent vertices and corresponding reference independent vertices are tracked using a fixed dimension handling algorithm [15]. The algorithm ensures that all incoming edges and outgoing edges of the dependent vertex are redirected to the corresponding reference vertex. Thus a dependent vertex is removed from the longest path. To handle connections between intra-layer (bond wires) and inter-layer (vias), a propagation dictionary is used, which provides the necessary propagation path from a child node to the common reference node. After propagating up to sub-root nodes, the longest path from the source and sink is propagated to the root as the root has only these two shared vertices.

4) Top-Down Location Propagation: Once the bottom-up constraint propagation is complete, the evaluated constraint graphs of the root node determine the minimum size of the structure. This minimum size (width, length) determines the location of the source and sink vertices of the sub-root nodes. The rest of the vertices locations are determined using the fixed floorplan handling algorithm described in [15]. If the algorithms are used for fixed-sized solution generation, this root node determines the maximum room for randomization by subtracting the minimum size from the fixed floorplan size provided by the user. The shared vertices locations are propagated from the parent node directly, whereas the rest of the independent vertices locations are determined from the constraint graph created for that node. The dependent vertex location is calculated as soon as the corresponding

---

**Algorithm 3: Via Propagation Dictionary Assignment**

```
1 Propagation_dict= {} 
2 for each via do 
3   Propagation_dict[via_name]=[corresponding sub-root node id (reference node id)] 
4   Propagation_dict[via_name].append(via node id) 
5   node id=via node id 
6 while node id is not equal to the reference node id 
7     Propagation_dict[via_name].append(node id) 
8     node id=id of the parent node 
9 return Propagation_dict
```
reference vertex location is determined. This algorithm gives a DRC-clean location range for each vertex in each node. All algorithms associated with the constraint graph evaluation have a time complexity $O(V+E)$, where $E$ and $V$ are the number of edges and vertices, respectively. Since the locations of connected vertices are determined by the common reference node, bonding wires, and vias are always aligned. Our proposed algorithms handle both 2D and 3D connections in a generic way. However, there are some fundamental differences between 2D/2.5D single-layer structure and multi-layer 3D structure handling. For example, in a multi-layer structure, the via-connected layers under a sub-root should have the same floorplan size. 2D/2.5D connection (i.e., bonding wires) handling algorithms require vertex sharing in either HCG or VCG, whereas in 3D cases, both HCG and VCG need to be considered simultaneously to handle via connections.

D. Layout Evaluation and Optimization

The algorithms are implemented to generate an arbitrary number of solutions. These solutions are evaluated with both electrical and thermal models. For electrical evaluation, a partial element equivalent circuit (PEEC)-based hierarchical RCLM model is used [17] for minimum-sized solutions. In addition to the built-in model, an electrical modeling interface has been built to export designs into FastHenry [18]. This interface has been used for evaluating a large solution space. To evaluate the static thermal performance, a 3D reduced-order multi-level RC network model is used by leveraging the application program interface (API) developed between PowerSynth and ParaPower [19].

1) Electrical Performance Evaluation: Electrical parasitics, primarily parasitic inductance, is one of the critical design parameters for MCPM to achieve high performance at high switching speed. In this paper, the PEEC model [17] has been further extended to support the 3D layout evaluation. For this purpose, an API has been developed to convert the layout geometrical information into an equivalent netlist for MCPM to achieve high performance at high switching speed. In this paper, the PEEC model [17] has been further extended to support the 3D layout evaluation. For this purpose, an API has been developed to convert the layout geometrical information into an equivalent netlist of R and L elements. The layout solution data is arranged into a table object, where each row of the table contains a set of trace groups. Depending on the structure of each layout group, three pre-defined orientations: vertical (V), horizontal (H), and planar (P). Using these pre-defined orientations, the meshing algorithm can efficiently generate the mesh for a single direction or multiple directions of current flows. The meshing algorithm loops through each trace group and convert them into equivalent mesh nodes and edges. A mesh node contains voltage information, while a mesh edge has the parasitic value R and L as its weight and contains current information. Once a mesh of all partial parasitic elements is formed, the modified nodal analysis (MNA) method is used to evaluate the loop inductance value. This model has shown good accuracy with FastHenry for the minimum-sized solution evaluation. However, this model is not matured enough for handling the optimization case, where the floorplan size changes dynamically. Therefore, in the case of optimization, FastHenry has been used for evaluating the loop inductance values of the generated solution space.

2) Thermal Performance Evaluation: Since the 3D structure is denser compared to the 2D one, thermal performance prediction is a critical aspect of optimization. In this work, static maximum temperature has been used as a thermal performance metric. ParaPower [19] is a thermal and stress evaluation tool developed by the Army Research Lab (ARL). An API has been developed to pass the layout solution structure to ParaPower and get the maximum temperature evaluated from it. In this tool, each structure is represented as a 3D box, and the boundary conditions can be applied to each arbitrary surface. All empty places in the volume of the structure are filled with air by default. The meshing precision is user-defined for each object. The complete structure is stored as a matrix, and the number of elements of the matrix is dependent on the meshing size defined by the user. An RC network is created for each element of the meshing, and each node of the network is evaluated in the specified time intervals. After a certain time period, each node temperature is stored in the result matrix. This temperature evaluation tool results have been verified against finite element analysis (FEA) tools like ANSYS Workbench, and significant speedup has been achieved within acceptable accuracy.

3) Layout Optimization: All generated solutions are evaluated using the aforementioned models, and the solution space is reported to choose the optimum solution. Though the randomization method has no guidance towards optimization, it can cover a large solution space if a large number of layout solutions are generated. Though a genetic algorithm can be implemented to find an optimal solution set for 2D layouts in comparatively faster than the randomization approach, the algorithm needs customization for handling 3D layouts as the design variables are exponentially increasing with the module geometry complexity. Therefore, a customized optimization algorithm study is on-going, and the randomization algorithm has been used until the best-suited optimization algorithm is developed. To report the Pareto-front solution space, a non-dominated sorting algorithm is applied to the complete solution space generated by the layout engine. From the Pareto-optimal solution set, the user can choose one point of interest and export the solution to the standard 3D modeling tools (i.e., SolidWorks, Ansys Q3D) through Powersynth export feature.

III. EXPERIMENTAL RESULTS

Since the designers have barely practiced the 3D power module layout design compared to the 2D cases, a performance comparison has been performed between a 2D half-bridge SiC power module and its 3D counterpart. Among many aspects, two essential but conflicting performance metrics like power loop inductance and maximum junction temperature of the module are considered for evaluation. Following the comparison, two hybrid 3D power module design cases are considered for electro-thermal performance evaluation.
A. 2D vs. 3D Performance Comparison

A 2D and a 3D half-bridge power module with two SiC MOSFETs per switching position are considered for electro-thermal performance comparison. Initial layouts for both of the cases are shown in Fig. 5. For a fair comparison, the 3D layout has been designed by splitting the 2D module into two layers: one is for the high-side switching, and the other is for the low-side switching. Both layers are stacked vertically, and a metallic post has been considered to have a via type connection in between them. The 3D structure with layout breakdown is shown in Fig. 5(b). In each layer floorplan figure, ‘V’ stands for the via type connection. For both 2D and 3D cases, a minimum-sized solution has been generated and evaluated by using PowerSynth. A set of standard design rules (i.e., min spacing, min enclosure, min width) have been considered for generating the solutions. The minimum-sized solution refers to the most compact and maximum achievable power density for a specific layout. The solution layouts are shown in Fig. 6. Power loop inductance at 100 kHz is 6.104 nH and 15.793 nH for 3D and 2D, respectively. From the figure, it is clear that the 3D power loop area is much smaller than that of 2D as the former one has a vertical loop, whereas the latter one has a planar loop. For thermal evaluation, ambient temperature is set to 300 K, heat dissipation for each die is 10 W. In the case of 2D configuration, only the bottom side of the baseplate, whereas for the 3D case, both top and bottom sides have been equipped with an effective heat transfer coefficient of 1000 W/m² – K. For 3D, and 2D cases, the maximum temperature for the devices are found 328.377 K, and 332.147 K, respectively. However, single-sided cooling with 1000 W/m² – K heat transfer coefficient makes the 3D case maximum temperature as high as 370.287 K. Therefore, for the compact 3D layout with less area for heat dissipation, double-sided cooling is a must to maintain low junction temperature compared to the 2D case. The results indicate that adding the third dimension to the MCPM layout design improves both electrical and thermal performance.

B. 3D Layout Optimization

Since the 3D power module is an emerging and advanced technology, there are very few references for the packaging topology, which are fabricated and tested. Therefore, we chose two half-bridge power modules to demonstrate our methodology performance.

1) Test Case 1 (A SiC Power Module): For the first case, we have considered two SiC devices per switching position and split the two switches into two layers. A 3D structure of the module and the corresponding power loop are shown in Fig. 7. A layer-wise breakdown layout has been shown in Fig. 8(a). Drain, gate, and Kelvin source connections for each device are on the same layer, and the sources are connected to the neighboring upper layer through metallic post connectors. Thus the whole half-bridge consists of four routing layers containing three terminals: DC+, OUT, and DC-. A via (V) is used to connect two layers (L2 and L3) of a direct bonded copper (DBC) substrate, which serves as the output. For this initial layout, a minimum-sized solution has been generated and evaluated. The solution is shown in Fig. 8(b). The metallic post connectors (device source connection) are treated as via in the layout generation algorithms as they serve a similar purpose in terms of connectivity. So, all those pads are of the same color in the figure. The power loop inductance for this case is 1.406 nH at 1000 kHz, and the maximum temperature is found 349.282 K. The boundary conditions are the same as the 3D case used for performance comparison with the 2D layout.

2) Test Case 2 (An IGBT Power Module): The schematic of this case and the corresponding 3D structure are shown in Fig. 9(a), (b), respectively. Four IGBTs and anti-parallel
Table I

<table>
<thead>
<tr>
<th>Layout ID</th>
<th>Inductance (nH)</th>
<th>Temperature (°K)</th>
<th>Size (mm × mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>1.44</td>
<td>334.11</td>
<td>34.5 × 16.5</td>
</tr>
<tr>
<td>B</td>
<td>2.22</td>
<td>328.13</td>
<td>37.0 × 24.0</td>
</tr>
<tr>
<td>C</td>
<td>2.43</td>
<td>324.62</td>
<td>42.0 × 26.5</td>
</tr>
</tbody>
</table>

To optimize the layout, around 2400 solutions are generated with varying floorplan sizes from 569.25 mm$^2$ to 1113 mm$^2$. For each floorplan size, 100 solutions are generated. FastHenry and ParaPower have been used for electro-thermal performance evaluation. The resultant 2D plot is shown in Fig. 12. The solution points are color mapped with the floorplan sizes. Three corner solutions are chosen to show the tradeoff between two objectives. These three solutions are marked in Fig. 12, and the layouts are shown in Fig. 13. The floorplan sizes and performance values for the three layouts are shown in Table I. The table shows that Layout A has the smallest size, which results in the highest temperature rise. On the other hand, Layout C has the largest footprint with the lowest temperature and higher inductance. The balanced solution is shown in Layout B with a better tradeoff. The runtime for layout generation is about 8 s/100 layouts and evaluation is about 286 s/100 layouts on an Intel®Silver 4114 CPU computer. This shows our tool flow is both accurate and efficient enough for orders-of-magnitude design productivity improvement.

IV. Conclusion and Future Work

We propose constraint-aware physical design synthesis and optimization algorithms for 3D MPCM designs that are generic and efficient to handle both intra-layer and inter-layer connections. Our algorithms are scalable and efficient enough to handle multi-layered 3D layouts with an arbitrary number of layers. Experimental results of the 3D power module layout further test our algorithms through optimized layout solutions. We will further validate our framework by fabricating 3D power modules designed and optimized with our CAD tools. This module-level design framework can be extended towards cabinet-level physical design and optimization. A customized optimization algorithm will also be implemented to have a better tradeoff among multiple conflicting objectives.

Acknowledgment

The authors would like to thank Dr. Fang Luo, Dr. Lauren Boteler, Tristan Evans and Shilpi Mukherjee for their help and suggestions.

References

Fig. 10. Planar view of routing layers in Fig. 9: high-side device layer (L1), high-side device source layer (L2), low-side device layer (L3), and low-side device source layer (L4).

Fig. 11. Minimum-sized solution (32×16.5) mm² of Fig. 10.

Fig. 12. Design solution space for the example design in Fig. 9


